Isabelle/HOL Exercises Lists

Replace, Reverse and Delete

Define a function replace, such that $replace \times y \times zs$ yields zs with every occurrence of x replaced by y.

```
consts replace :: "'a \Rightarrow 'a  'a  list \Rightarrow 'a  list"
```

Prove or disprove (by counterexample) the following theorems. You may have to prove some lemmas first.

```
theorem "rev(replace x y zs) = replace x y (rev zs)"
theorem "replace x y (replace u v zs) = replace u v (replace x y zs)"
theorem "replace y z (replace x y zs) = replace x z zs"
```

Define two functions for removing elements from a list: $dell\ x\ xs$ deletes the first occurrence (from the left) of x in xs, $delall\ x\ xs$ all of them.

```
consts del1 :: "'a \Rightarrow 'a list \Rightarrow 'a list" dela11 :: "'a \Rightarrow 'a list \Rightarrow 'a list"
```

Prove or disprove (by counterexample) the following theorems.

```
theorem "del11 x (dela11 x xs) = dela11 x xs"

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theorem "replace x y (del111 x zs) = del11 x zs"

theorem "replace x y (del111 x zs) = del11 z (replace x y zs)"

theorem "rev(del11 x xs) = del11 x (rev xs)"

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