

**theory** *SALMemPlatform* = *SALOverflowPlatform*:

## 1 SAL Memory Platform

— This platform accepts programs that are types safe, do not cause arithmetics overflows and do not use memory addresses outside  $[0, \text{MAXMEM}]$ .

### 1.1 Platform Definition

**constdefs**

*MAXMEM* :: *nat*

*MAXMEM*  $\equiv$  20

**constdefs**

*safeFm* :: *SALprogram*  $\Rightarrow$  *pos*  $\Rightarrow$  *SALform*

*safeFm* *prg* *pc*  $\equiv$

(*let* (*pn,i*) = *pc* *in*

(*case* (*cmd* *prg* *pc*)

*of None*  $\Rightarrow$  *FalseF*

| *Some ins*  $\Rightarrow$

(*case* *ins*

*of SET* *x n*  $\Rightarrow$  ( $\lambda$  (*p, m, e*). *x* < *MAXMEM*)

| *ADD* *x y*  $\Rightarrow$  ( $\lambda$  (*p, m, e*). *x* < *MAXMEM*  $\wedge$  *y* < *MAXMEM*)

| *SUB* *x y*  $\Rightarrow$  ( $\lambda$  (*p, m, e*). *x* < *MAXMEM*  $\wedge$  *y* < *MAXMEM*)

| *INC* *x*  $\Rightarrow$  ( $\lambda$  (*p, m, e*). *x* < *MAXMEM*)

| *JMPEQ* *x y t*  $\Rightarrow$  ( $\lambda$  (*p, m, e*). *x* < *MAXMEM*  $\wedge$  *y* < *MAXMEM*)

| *JMPL* *x y t*  $\Rightarrow$  ( $\lambda$  (*p, m, e*). *x* < *MAXMEM*  $\wedge$  *y* < *MAXMEM*)

| *JLE* *x y t*  $\Rightarrow$  ( $\lambda$  (*p, m, e*). *x* < *MAXMEM*  $\wedge$  *y* < *MAXMEM*)

| *JMPB* *t*  $\Rightarrow$   $\lambda$  (*p,m,e*). *True*

| *CALL* *x pn'*  $\Rightarrow$  ( $\lambda$  (*p, m, e*). *x* < *MAXMEM*)

| *RET* *x*  $\Rightarrow$  ( $\lambda$  (*p, m, e*). *x* < *MAXMEM*)

| *MOV* *s t*  $\Rightarrow$  ( $\lambda$  (*p, m, e*). ( $\forall$  *ns. m s* = *NAT ns*  $\longrightarrow$  *ns* < *MAXMEM*)  $\wedge$   
( $\forall$  *nt. m t* = *NAT nt*  $\longrightarrow$  *nt* < *MAXMEM*))

| *HALT*  $\Rightarrow$   $\lambda$  (*p,m,e*). *True*

)

)

)

**constdefs**

*safeF*:: *SALprogram*  $\Rightarrow$  *pos*  $\Rightarrow$  *SALform*

*safeF* *prg* *p*  $\equiv$  *Conj* [(*SALSafetyLogic.safeF* *prg* *p*), *safeFm* *prg* *p*]

**lemma**[*code*]:

*safeF* *prg* *p*  $\equiv$  *let* *a*=(*SALSafetyLogic.safeF* *prg* *p*); *b*=(*safeFm* *prg* *p*)

*in (term (Conj [(to-term a),(to-term b)]))*

**apply** (*simp only: safeF-def to-term-def term-def Let-def*)  
**done**

**constdefs**

*vcgSALm* :: *SALprogram*  $\Rightarrow$  *SALform*  
*vcgSALm prg*  $\equiv$  *vcG Conj Impl FalseF ipc initF safeF succsF wpF domC domA anF prg*

**generate-code** (*vcgSALT.ML*) [*term-of*]  
*vcg* = *vcgSALT*

**constdefs**

*isafeF*::*SALprogram*  $\Rightarrow$  *pos*  $\Rightarrow$  *SALform*  
*isafeF prg pc*  $\equiv$  *isafe(domC prg,prg,anF prg,pc,FalseF,Conj,Impl,safeF,succsF,wpF)*

**constdefs**

*isafeP*::*SALprogram*  $\Rightarrow$  *SALstate set* (*isafe* <sub>$\square$</sub> - [70])  
*isafeP prg*  $\equiv$  (*isafeP' effS valid initF isafeF prg*)

**lemma** *isafeP-induct*:

$\llbracket s \in (\text{isafeP prg});$   
 $\bigwedge s. \llbracket \text{valid prg } s (\text{initF prg}) \rrbracket \Longrightarrow P s;$   
 $\bigwedge s s'. \llbracket s \in (\text{isafeP prg}); \text{valid prg } s (\text{isafeF prg } (\text{fst } s)); \text{valid prg } s' (\text{isafeF prg } (\text{fst } s')); (s,s') \in (\text{effS prg}); P s \rrbracket \Longrightarrow P s' \rrbracket \Longrightarrow P \text{sdone}$

**constdefs**

*provable* :: *SALprogram*  $\Rightarrow$  *SALform*  $\Rightarrow$  *bool* ((-  $\vdash$  -) [61,60] 60)  
*provable prg f*  $\equiv$   $\forall s. s \in (\text{isafeP prg}) \longrightarrow \text{valid prg } s f$   
**end**